

1 **Draft NIST Special Publication 800-185**
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3 **SHA-3 Derived Functions:**
4 *cSHAKE, KMAC, TupleHash and ParallelHash*

5
6 John Kelsey
7 Shu-jen Chang
8 Ray Perlner
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11 C O M P U T E R S E C U R I T Y
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John Kelsey
Shu-jen Chang
Ray Perlner
*Computer Security Division
Information Technology Laboratory*

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August 2016

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63 **National Institute of Standards and Technology Special Publication 800-185**

64 Natl. Inst. Stand. Technol. Spec. Publ. 800-185, 30 pages (August 2016)

65 CODEN: NSPUE2

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80 **Public comment period: August 4, 2016 through September 30, 2016**

81 National Institute of Standards and Technology
82 Attn: Computer Security Division, Information Technology Laboratory
83 100 Bureau Drive (Mail Stop 8930) Gaithersburg, MD 20899-8930
84 Email: SP800-185@nist.gov

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99

Abstract

100 This Recommendation specifies four types of SHA-3-derived function: cSHAKE, KMAC,
101 TupleHash, and ParallelHash, each defined for a 128- and 256-bit security level. cSHAKE is a
102 customizable variant of the SHAKE function, as defined in FIPS 202. KMAC (for KECCAK
103 Message Authentication Code) is a variable-length message authentication code algorithm based
104 on KECCAK; it can also be used as a pseudorandom function. TupleHash is a variable-length hash
105 function designed to hash tuples of input strings without trivial collisions. ParallelHash is a
106 variable-length hash function that can hash very long messages in parallel.

107

Keywords

108 authentication; cryptography; cSHAKE; customizable SHAKE function; hash function;
109 information security; integrity; KECCAK; KMAC; message authentication code; parallel hashing;
110 ParallelHash; PRF; pseudorandom function; SHA-3; SHAKE; tuple hashing; TupleHash.

111

Acknowledgements

113 The authors thank the KECCAK team members: Guido Bertoni, Joan Daemen, Michaël Peeters,
114 and Gilles Van Assche. The authors also thank their colleagues that reviewed drafts of this
115 document and contributed to its development.

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Table of Contents

| | | |
|-----|---|----|
| 119 | 1 Introduction | 1 |
| 120 | 2 Glossary | 3 |
| 121 | 2.1 Terms and Acronyms | 3 |
| 122 | 2.2 Basic Operations | 4 |
| 123 | 2.3 Other Internal Functions | 4 |
| 124 | 2.3.1 Integer to Byte String Encoding..... | 4 |
| 125 | 2.3.2 String Encoding | 5 |
| 126 | 2.3.3 Padding | 6 |
| 127 | 2.3.4 Substrings | 6 |
| 128 | 3 cSHAKE | 7 |
| 129 | 3.1 Overview..... | 7 |
| 130 | 3.2 Parameters | 7 |
| 131 | 3.3 Definition..... | 8 |
| 132 | 3.4 Using the Customization String | 8 |
| 133 | 3.5 Using the Function Name Input | 9 |
| 134 | 4 KMAC | 10 |
| 135 | 4.1 Overview..... | 10 |
| 136 | 4.2 Parameters | 10 |
| 137 | 4.3 Definition..... | 10 |
| 138 | 4.3.1 KMAC with Arbitrary-Length Output | 11 |
| 139 | 5 TupleHash | 12 |
| 140 | 5.1 Overview..... | 12 |
| 141 | 5.2 Parameters | 12 |
| 142 | 5.3 Definition..... | 12 |
| 143 | 5.3.1 TupleHash with Arbitrary-Length Output | 13 |
| 144 | 6 ParallelHash | 14 |
| 145 | 6.1 Overview..... | 14 |
| 146 | 6.2 Parameters | 14 |
| 147 | 6.3 Definition..... | 14 |
| 148 | 6.3.1 ParallelHash with Arbitrary-Length Output | 15 |
| 149 | 7 Implementation Considerations | 16 |

| | | |
|-----|---|-----------|
| 150 | 7.1 Precomputation | 16 |
| 151 | 7.2 Limited Implementations..... | 16 |
| 152 | 7.3 Exploiting Parallelism in ParallelHash | 16 |
| 153 | 8 Security Considerations | 18 |
| 154 | 8.1 Security Properties for Name and Customization String..... | 18 |
| 155 | 8.1.1 Equivalent Security to SHAKE for Any Legal S and N..... | 18 |
| 156 | 8.1.2 Different S and N Give Unrelated Functions..... | 18 |
| 157 | 8.2 Claimed Security Level..... | 18 |
| 158 | 8.3 Collisions and Preimages | 19 |
| 159 | 8.4 Guidance for Using KMAC Securely..... | 19 |
| 160 | 8.4.1 KMAC Key Length | 19 |
| 161 | 8.4.2 KMAC Output Length | 19 |
| 162 | | |
| 163 | List of Appendices | |
| 164 | Appendix A— KMAC, TupleHash, and ParallelHash in Terms of KECCAK[c]..... | 21 |
| 165 | Appendix B— Hashing into a Range (Informative)..... | 23 |
| 166 | Appendix C— References | 24 |
| 167 | | |
| 168 | List of Tables | |
| 169 | Table 1: Equivalent security settings for KMAC and previously standardized MAC | |
| 170 | algorithms..... | 19 |
| 171 | | |

172 **1 Introduction**

173 Federal Information Processing Standard (FIPS) 202, *SHA-3 Standard: Permutation-Based Hash*
 174 *and Extendable-Output Functions* [1], defines four fixed-length hash functions (SHA3-224,
 175 SHA3-256, SHA3-384, and SHA3-512), and two eXtendable Output Functions (XOFs),
 176 SHAKE128 and SHAKE256. These SHAKE functions are a new kind of cryptographic
 177 primitive; unlike earlier hash functions, they are named for their expected security level.

178 FIPS 202 also supports a flexible scheme for domain separation between different functions
 179 derived from KECCAK—the algorithm [2] that the SHA-3 Standard is based on. Domain
 180 separation ensures that different named functions (such as SHA3-512 and SHAKE128) will be
 181 unrelated. cSHAKE—the customizable version of SHAKE—extends this scheme to allow users
 182 to customize their use of the function, as described below.

183 Customization is analogous to strong typing in a programming language; such customization
 184 makes it extremely unlikely that computing one function with two different customization strings
 185 will yield the same answer. Thus, two cSHAKE computations with different customization
 186 strings (for example, a key fingerprint and an email signature) are unrelated: knowing one of
 187 these results will give an attacker no information about the other.

188 This Recommendation defines two cSHAKE variants, cSHAKE128 and cSHAKE256, in Sec. 3,
 189 based on the KECCAK[*c*] sponge function [3] defined in FIPS 202. It then defines three additional
 190 SHA-3-derived functions, in Secs. 4 through 6, that provide new functionality not directly
 191 available from the more basic functions. They are:

- 192 • KMAC128 and KMAC256, providing pseudorandom functions (PRFs) and keyed hash
 193 functions with variable-length outputs;
- 194 • TupleHash128 and TupleHash256, providing functions that hash tuples of input strings
 195 correctly and unambiguously¹; and
- 196 • ParallelHash128 and ParallelHash256, providing efficient hash functions to hash long
 197 messages more quickly by taking advantage of parallelism in the processors.

198 All four functions defined in this Recommendation—cSHAKE, KMAC, TupleHash, and
 199 ParallelHash—have these properties in common:

- 200 • They are all derived from the functions specified in FIPS 202.
- 201 • All the functions except cSHAKE are defined in terms of cSHAKE.
- 202 • All support user-defined customization strings.
- 203 • All support variable-length outputs of any bit length, with the additional property that any
 204 change in the requested output length completely changes the function. Even with

¹ TupleHash processes a tuple of one or more input strings, and incorporates the contents of all the strings, the number of strings, and the specific content of each string in the calculation of the resulting hash value. Thus, any change (such as moving bytes from one input string to an adjacent one, or removing an empty string from the input tuple) is extremely likely to lead to a different result.

205 identical inputs otherwise, any of these functions, when called with different requested
206 output lengths, will, in general, yield unrelated outputs.

- 207 • All support two security levels: 128 and 256 bits.

208 These functions are detailed in the specific sections below. In addition, a method is specified in
209 Appendix B to facilitate using these functions to produce output that is almost uniformly
210 distributed on the integers $\{0, 1, 2, \dots, R-1\}$.

211

212 **2 Glossary**

213 In this document, bits are indicated in the *Courier New* font. Bytes are typically written as two-digit hexadecimal numbers from the ASCII characters 0 through 9 and A through F, preceded by
 214 the prefix “0x”. In binary representation, bytes are written with the low-order bit first, while in
 215 hexadecimal representation, bytes are written with the high-order digit first. E.g., 0x01 =
 216 10000000 and 0x80 = 00000001. These bit-ordering conventions follow the conventions
 217 established in Sec. B.1 of FIPS 202. Character strings appear in this document in double-quotes.
 218 Character strings are interpreted as bit strings whose length is a multiple of 8 bits, consisting of a
 219 0 bit, followed by the 7-bit ASCII representation of each successive character.

221 **2.1 Terms and Acronyms**

| | |
|----------------------------------|---|
| Bit | A binary digit: 0 or 1. |
| CMAC | Cipher-based Message Authentication Code. |
| cSHAKE | The customizable SHAKE function. |
| Domain Separation | For a function, a partitioning of the inputs to different application domains so that no input is assigned to more than one domain. |
| eXtendable-Output Function (XOF) | A function on bit strings in which the output can be extended to any desired length. |
| FIPS | Federal Information Processing Standard. |
| Hash Function | A function on bit strings in which the length of the output is fixed. The output often serves as a condensed representation of the input. |
| HMAC | Keyed-Hash Message Authentication Code. |
| KECCAK | The family of all sponge functions with a KECCAK- <i>f</i> permutation as the underlying function and multi-rate padding as the padding rule. KECCAK was originally specified in [2], and standardized in FIPS 202. |
| KMAC | KECCAK Message Authentication Code. |
| MAC | Message Authentication Code. |
| NIST | National Institute of Standards and Technology. |
| PRF | See <i>Pseudorandom Function</i> . |
| Pseudorandom Function | A function that can be used to generate output from a random seed such that the output is computationally indistinguishable |

| | |
|---------------------|--|
| (PRF) | from truly random output. |
| Rate | In the sponge construction, the number of input bits processed per invocation of the underlying function. |
| SHA-3 | Secure Hash Algorithm-3. |
| Sponge Construction | The method originally specified in [3] for defining a function from the following: 1) an underlying function on bit strings of a fixed length, 2) a padding rule, and 3) a rate. Both the input and the output of the resulting function are bit strings that can be arbitrarily long. |
| Sponge Function | A function that is defined according to the sponge construction, possibly specialized to a fixed output length. |
| String | A sequence of bits. |
| XOF | See <i>eXtendable-Output Function</i> . |

222 2.2 Basic Operations

| | |
|--------------------|--|
| [x] | For a real number x , $[x]$ is the least integer that is not strictly less than x . For example, $[3.2] = 4$, $[-3.2] = -3$, and $[6] = 6$. |
| 0^s | For a positive integer s , 0^s is the string that consists of s consecutive 0 bits. |
| $\text{enc}_8(i)$ | For an integer i ranging from 0 to 255, $\text{enc}_8(i)$ is the byte encoding of i , with bit 0 being the low-order bit of the byte. |
| $\text{len}(X)$ | For a bit string X , $\text{len}(X)$ is the length of X in bits. |
| $\text{mod}(a, b)$ | The modulo operation. $\text{mod}(a, b)$ returns the remainder after division of a by b . |
| $X \parallel Y$ | For strings X and Y , $X \parallel Y$ is the concatenation of X and Y . For example, $11001 \parallel 010 = 11001010$. |

223 2.3 Other Internal Functions

- 224 This section describes the string encoding, padding and substring functions used in the definition of the SHA-3-derived functions.
- 226 **2.3.1 Integer to Byte String Encoding**
- 227 Two internal functions, *left_encode* and *right_encode*, are defined to encode integers as byte

228 strings. Both functions can encode integers up to an extremely large maximum, $2^{2040}-1$.

229 `left_encode(x)` encodes the integer x as a byte string in a way that can be unambiguously parsed
 230 from the beginning of the string by inserting the length of the byte string before the byte string
 231 representation of x .

232 `right_encode(x)` encodes the integer x as a byte string in a way that can be unambiguously parsed
 233 from the end of the string by inserting the length of the byte string after the byte string
 234 representation of x .

235 Using the function `enc8()` to encode the individual bytes, these two functions are defined as
 236 follows:

237 **`right_encode(x):`**
 238 *Validity Conditions:* $0 \leq x < 2^{2040}$

- 239 1. Let n be the smallest integer for which $2^{8n} > x$.
- 240 2. Let x_1, x_2, \dots, x_n be the base-256 encoding of x satisfying:

$$x = \sum 2^{8(n-i)}x_i, \text{ for } i = 1 \text{ to } n.$$
- 241 3. Let $O_i = \text{enc8}(x_i)$, for $i = 1$ to n .
- 242 4. Let $O_{n+1} = \text{enc8}(n)$.
- 243 5. Return $O = O_1 \parallel O_2 \parallel \dots \parallel O_n \parallel O_{n+1}$.

244 **`left_encode(x):`**
 245 *Validity Conditions:* $0 \leq x < 2^{2040}$

- 246 1. Let n be the smallest integer for which $2^{8n} > x$.
- 247 2. Let x_1, x_2, \dots, x_n be the base-256 encoding of x satisfying:

$$x = \sum 2^{8(n-i)}x_i, \text{ for } i = 1 \text{ to } n.$$
- 248 3. Let $O_i = \text{enc8}(x_i)$, for $i = 1$ to n .
- 249 4. Let $O_0 = \text{enc8}(n)$.
- 250 5. Return $O = O_0 \parallel O_1 \parallel \dots \parallel O_{n-1} \parallel O_n$.

251 **2.3.2 String Encoding**

252 The `encode_string` function is used to encode bit strings in a way that may be parsed
 253 unambiguously from the beginning of the string, S . The function is defined as follows:

254 **`encode_string(S):`**
 255 *Validity Conditions:* $0 \leq \text{len}(S) < 2^{2040}$

- 256 1. Return `left_encode(len(S)) || S`.

257 Note that if the bit string S is not byte-oriented (i.e., $\text{len}(S)$ is not a multiple of 8), the bit string
 258 returned from `encode_string(S)` is also not byte-oriented. However, if $\text{len}(S)$ is a multiple of 8,
 259 then the length of the output of `encode_string(S)` will also be a multiple of 8.

266 **2.3.3 Padding**

267 The `bytepad(X, w)` function pads an input string X with zeros until it is a byte string whose length
 268 in bytes is a multiple of w . In general, `bytepad` is intended to be used on encoded strings—the
 269 byte string `bytepad(encode_string(S), w)` can be parsed unambiguously from its beginning,
 270 whereas `bytepad` does not provide unambiguous padding for all input strings.

271 The definition of `bytepad()` is as follows:

272 **bytepad(X, w):**

273 *Validity Conditions:* $w > 0$

274

275 1. $z = \text{left_encode}(w) \parallel X$.

276 2. while $\text{len}(z) \bmod 8 \neq 0$:

277 $z = z // 0$

278 3. while $(\text{len}(z)/8) \bmod w \neq 0$:

279 $z = z \parallel 00000000$

280 4. return z .

281 **2.3.4 Substrings**

282 Let parameters a and b be non-negative integers that denote a specific position in a bit string X .
 283 Informally, the `substring(X, a, b)` function returns a substring from the bit string X containing the
 284 values at positions $a, a+1, \dots, b-1$, inclusive. More precisely, the `substring` function operates as
 285 defined below. Note that all bit positions in the input and output strings are indexed from zero.
 286 Thus, the first bit in a string is in position 0, and the last bit in an n -bit string is in position $n-1$.

287

288 **substring(X, a, b):**

289

290 1. If $a \geq b$ or $a \geq \text{len}(X)$:

291 return the empty string.

292 2. Else if $b \leq \text{len}(X)$:

293 return the bits of X from position a to position $b-1$, inclusive.

294 3. Else:

295 return the bits of X from position a to position $\text{len}(X)-1$, inclusive.

297 **3 cSHAKE**298 **3.1 Overview**

299 The two variants of cSHAKE—cSHAKE128 and cSHAKE256—are defined in terms of the
300 SHAKE and KECCAK[*c*] functions specified in FIPS 202. cSHAKE128 provides a 128-bit
301 security level, while cSHAKE256 provides a 256-bit security level.

302 **3.2 Parameters**

303 Both cSHAKE functions take four parameters:

- 304 • *X* is the main input bit string. It may be of any length, including zero.
- 305 • *L* is an integer representing the requested output length, in bits.
- 306 • *S* is a customization bit string. The user selects this string to define a variant of the
307 function. When no customization is desired, *S* is set to the empty string².
- 308 • *N* is a function-name bit string, used by NIST to define functions based on cSHAKE.
309 When no function other than cSHAKE is desired, *N* is set to the empty string.

310 An implementation of cSHAKE may reasonably support only input strings and output lengths
311 that are whole bytes; if so, a fractional-byte input string or a request for an output length that is
312 not a multiple of 8 would result in an error.

313 When *S* and *N* are both empty strings, cSHAKE(*X, L, S, N*) is equivalent to SHAKE as defined in
314 FIPS 202. Thus,

$$\begin{aligned} 315 \quad \text{cSHAKE128}(X, L, "", "") &= \text{SHAKE128}(X, L) \text{ and} \\ 316 \quad \text{cSHAKE256}(X, L, "", "") &= \text{SHAKE256}(X, L). \end{aligned}$$

317 cSHAKE is designed so that for any two instances:

$$\begin{aligned} 318 \quad \text{cSHAKE}(X_1, L_1, S_1, N_1) \text{ and} \\ 319 \quad \text{cSHAKE}(X_1, L_1, S_2, N_2), \end{aligned}$$

320 unless *S*₁ = *S*₂ and *N*₁ = *N*₂, the two instances produce unrelated outputs. Note that this includes
321 the case where *S*₁ and *N*₁ are empty strings. That is, cSHAKE with any customization is domain-
322 separated from the ordinary SHAKE function specified in FIPS 202.

² In computing languages that support default values for parameters, a natural way to implement this function would set the default values for *S* and *N* to empty strings.

323 **3.3 Definition**

324 cSHAKE is defined in terms of SHAKE or KECCAK[c], as follows: it either returns the result of a
 325 call to SHAKE (if S and N are both empty strings), or returns the result of a call to KECCAK(c)
 326 with a padded encoding of S and N concatenated to the input string X .

327 **cSHAKE128(X, L, S, N):**

328 *Validity Conditions:* $\text{len}(S) < 2^{2040}$ and $\text{len}(N) < 2^{2040}$

329
 330 1. If $S = ""$ and $N = ""$:
 331 return SHAKE128(X, L);
 332 2. Else:
 333 return KECCAK[256](bytepad(encode_string(S) || encode_string(N), 168) || X || 00, L).
 334

335 **cSHAKE256(X, L, S, N):**

336 *Validity Conditions:* $\text{len}(S) < 2^{2040}$ and $\text{len}(N) < 2^{2040}$

337
 338 1. If $S = ""$ and $N = ""$:
 339 return SHAKE256(X, L);
 340 2. Else:
 341 return KECCAK[512](bytepad(encode_string(S) || encode_string(N), 136) || X || 00, L).
 342

343 Note that the numbers 168 and 136 are *rates* (in bytes) of the KECCAK[256] and KECCAK[512]
 344 sponge functions, respectively; and the characters 00 in the Courier New font in these
 345 definitions specify two zero bits.

346 **3.4 Using the Customization String**

347 The cSHAKE function includes an input string (S) to allow users to customize their use of the
 348 function. For example, someone using cSHAKE128 to compute a key fingerprint (the hash value
 349 for a public key) might use:

350 cSHAKE128(*public_key*, 256, "key fingerprint", ""),

351 where "key fingerprint" is a customization string S .

352 Later, the same user might decide to customize a different cSHAKE computation for signing an
 353 email:

354 cSHAKE128(*email_contents*, 256, "email signature", ""),

355 where "email signature" is the customization string S .

356 The customization string is intended to avoid a collision between these two cSHAKE values—it
 357 will never be possible for an attacker to somehow use one computation (the email signature) to
 358 get the result of the other computation (the key fingerprint) if different values of S are used.

359 The customization string may be of any length less than 2^{2040} ; however, implementations may

360 restrict the length of S that they will accept.

361 **3.5 Using the Function Name Input**

362 The cSHAKE function also includes an input string that may be used to provide a function name
363 (N). This is intended for use by NIST in defining SHA-3-derived functions, and should only be
364 set to values defined by NIST. This parameter provides a level of domain separation by function
365 name. Users of cSHAKE should not make up their own names—that kind of customization is the
366 purpose of the customization string S . Nonstandard values of N could cause interoperability
367 problems with future NIST-defined functions.

368

369 **4 KMAC**370 **4.1 Overview**

371 The KECCAK Message Authentication Code (KMAC) algorithm is a PRF and keyed hash
 372 function based on KECCAK. It provides variable-length output, and unlike SHAKE and cSHAKE,
 373 altering the requested output length generates a new, unrelated output. KMAC has two variants,
 374 KMAC128 and KMAC256, built from cSHAKE128 and cSHAKE256, respectively. The two
 375 variants differ somewhat in their technical security properties. Nonetheless, for most
 376 applications, both variants can support any security level up to 256 bits of security, provided that
 377 a long enough key is used, as discussed in Sec. 8.4.1 below.

378 **4.2 Parameters**

379 Both KMAC functions take the following parameters:

- 380 • K is a key bit string of any length, including zero.
- 381 • X is the main input bit string. It may be of any length, including zero.
- 382 • L is an integer representing the requested output length³ in bits.
- 383 • S is an optional customization bit string of any length, including zero. If no customization
 384 is desired, S is set to the empty string.

385 **4.3 Definition**

386 KMAC concatenates a padded version of the key K with the input X and an encoding of the
 387 requested output length L . The result is then passed to cSHAKE, along with the requested output
 388 length L , the optional customization string S , and the name $N = "KMAC" = 01001011$
 389 $01001101\ 01000001\ 01000011$.

390 **KMAC128(K, X, L, S):**

391 *Validity Conditions:* $\text{len}(K) < 2^{2040}$ and $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 392
- 393 1. $\text{new}X = \text{bytepad}(\text{encode_string}(K), 168) \parallel X \parallel \text{right_encode}(L).$
 - 394 2. return cSHAKE128($\text{new}X, L, S, "KMAC"$).

395

396 **KMAC256(K, X, L, S):**

397 *Validity Conditions:* $\text{len}(K) < 2^{2040}$ and $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 398
- 399 1. $\text{new}X = \text{bytepad}(\text{encode_string}(K), 136) \parallel X \parallel \text{right_encode}(L).$
 - 400 2. return cSHAKE256($\text{new}X, L, S, "KMAC"$).

401

³ Note that there is a limit of $2^{2040}-1$ bits of output from this function unless the function is used as a XOF, as discussed in Sec. 4.3.1.

402 Note that the numbers 168 and 136 are *rates* (in bytes) of the KECCAK[256] and KECCAK[512]
403 sponge functions, respectively.

404 **4.3.1 KMAC with Arbitrary-Length Output**

405 Some applications of KMAC may not know the number of output bits they will need until after
406 the outputs begin to be produced. For these applications, KMAC can also be used as a XOF (i.e.,
407 the output can be extended to any desired length) which mimics the behavior of cSHAKE.

408 When used as a XOF, KMAC is computed by setting the encoded output length L to 0.
409 Conceptually, when called with an encoded length of zero, KMAC produces an infinite-length
410 output string, and the caller simply uses as many bits of the output string as are needed.

411

412 **5 TupleHash**413 **5.1 Overview**

414 TupleHash is a SHA-3-derived hash function with variable-length output that is designed to
 415 simply and correctly hash a tuple of input strings, any or all of which may be empty strings. Such
 416 a tuple may consist of any number of strings, including zero, and is represented as a sequence of
 417 strings or variables in parentheses like (a, b, c, \dots, z) in this document.

418 TupleHash is designed to provide a generic, misuse-resistant way to combine a sequence of
 419 strings for hashing such that, for example, a TupleHash computed on the tuple ("abc", "d") will
 420 produce a different hash value than a TupleHash computed on the tuple ("ab", "cd"), even though
 421 all the remaining input parameters are kept the same, and the two resulting concatenated strings,
 422 without string encoding, are identical.

423 TupleHash supports two security levels: 128 bits and 256 bits. Changing any input to the
 424 function, including the requested output length, will almost certainly change the final output.

425 **5.2 Parameters**

426 TupleHash takes the following parameters:

- 427 • X is a tuple of zero or more bit strings, any or all of which may be an empty string.
- 428 • L is an integer representing the requested output length, in bits.
- 429 • S is an optional customization bit string of any length, including zero. If no customization
 430 is desired, S is set to the empty string.

431 **5.3 Definition**

432 TupleHash encodes the sequence of input strings in an unambiguous way, then encodes the
 433 requested output length at the end of the string, and passes the result into cSHAKE, along with
 434 the function name (N) of “TupleHash” = 01010100 01110101 01110000 01101100
 435 01100101 01001000 01100001 01110011 01101000.

436 If X is a tuple of n bit strings, let $X[i]$ be the i th bit string, numbering from 0. The TupleHash
 437 functions are defined in pseudocode as follows:

438 **TupleHash128(X, L, S):**

439 *Validity Conditions:* $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 440 1. $z = ""$.
- 441 2. n = the number of input strings in the tuple X .
- 442 3. for $i = 1$ to n :
 443 $z = z \parallel \text{encode_string}(X[i])$.
- 444 4. $\text{new}X = z \parallel \text{right_encode}(L)$.
- 445 5. return cSHAKE128($\text{new}X, L, S$, “TupleHash”).

447 **TupleHash256(X, L, S):**
448 *Validity Conditions:* $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$
449
450 1. $z = ""$.
451 2. $n =$ the number of input strings in the tuple X .
452 3. for $i = 1$ to n :
453 $z = z \parallel \text{encode_string}(X[i])$.
454 4. $\text{new}X = z \parallel \text{right_encode}(L)$.
455 5. return cSHAKE256($\text{new}X, L, S$, “TupleHash”).

456 **5.3.1 TupleHash with Arbitrary-Length Output**

457 Some applications of TupleHash may not know the number of output bits they will need until
458 after the outputs begin to be produced. For these applications, TupleHash can also be used as a
459 XOF (i.e., the output can be extended to any desired length) which mimics the behavior of
460 cSHAKE.

461 When used as a XOF, TupleHash is computed by setting the encoded output length L to 0.
462 Conceptually, when called with an encoded length of zero, TupleHash produces an infinite-
463 length output string, and the caller simply uses as many bits of the output string as are needed.

464

465 **6 ParallelHash⁴**466 **6.1 Overview**

467 The purpose of ParallelHash is to support the efficient hashing of very long strings, by taking
 468 advantage of the parallelism available in modern processors. ParallelHash supports the 128- and
 469 256-bit security levels, and also provides variable-length output. Changing any input parameter
 470 to ParallelHash, even the requested output length, will result in unrelated output. Like the other
 471 functions defined in this document, ParallelHash also supports user-selected customization
 472 strings.

473 **6.2 Parameters**

474 ParallelHash takes the following parameters:

- 475 • X is the main input bit string. It may be of any length, including zero.
- 476 • B is the block size in bytes for parallel hashing. It may be any integer > 0 .
- 477 • L is an integer representing the requested output length, in bits.
- 478 • S is an optional customization bit string of any length, including zero. If no customization
 is desired, S is set to the empty string.

480 **6.3 Definition**

481 ParallelHash divides the input bit string X into a sequence of non-overlapping blocks, each of
 482 length B bytes, and then computes the hash value for each block separately. Finally, these hash
 483 values are combined and hashed to generate the final hash value of the function. The name field
 484 N of cSHAKE is set to "ParallelHash" = 01010000 01100001 01110010 01100001
 485 01101100 01101100 01100101 01101100 01001000 01100001 01110011
 486 01101000.

487 The ParallelHash functions are defined in pseudocode as follows:

488 **ParallelHash128(X, B, L, S):**

489 *Validity Conditions:* $0 < B < 2^{2040}$ and $\lceil \text{len}(X)/B \rceil < 2^{2040}$ and
 490 $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 492 1. $n = \lceil (\text{len}(X)/8) / B \rceil$.
- 493 2. $z = \text{left_encode}(B)$.
- 494 3. $i = 0$.
- 495 4. for $i = 0$ to $n-1$:
 496 $z = z \parallel \text{cSHAKE128}(\text{substring}(X, i*B*8, (i+1)*B*8), 256, "", "")$.

⁴ A generic parallel hash mode for other NIST-approved hash functions may be developed in the future. The function here (i.e., ParallelHash) is specifically based on cSHAKE, and thus, on KECCAK.

498 5. $z = z \parallel \text{right_encode}(n) \parallel \text{right_encode}(L)$.
 499 6. $\text{newX} = z$.
 500 7. return cSHAKE128(newX, L, S , “ParallelHash”).

501 **ParallelHash256(X, B, L, S):**

502 *Validity Conditions:* $0 < B < 2^{2040}$ and $\lceil \text{len}(X)/B \rceil < 2^{2040}$ and
 503 $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

504
 505 1. $n = \lceil (\text{len}(X)/8) / B \rceil$.
 506 2. $z = \text{left_encode}(B)$.
 507 3. $i = 0$.
 508 4. for $i = 0$ to $n-1$:
 $z = z \parallel \text{cSHAKE256}(\text{substring}(X, i*B*8, (i+1)*B*8), 512, "", "")$.
 509 5. $z = z \parallel \text{right_encode}(n) \parallel \text{right_encode}(L)$.
 510 6. $\text{newX} = z$.
 511 7. return cSHAKE256(newX, L, S , “ParallelHash”).

513 **6.3.1 ParallelHash with Arbitrary-Length Output**

514 Some applications of ParallelHash may not know the number of output bits they will need until
 515 after the outputs begin to be produced. For these applications, ParallelHash can also be used as a
 516 XOF (i.e., the output can be extended to any desired length) which mimics the behavior of
 517 cSHAKE.

518 When used as a XOF, ParallelHash is computed by setting the encoded output length L to 0.
 519 Conceptually, when called with an encoded length of zero, ParallelHash produces an infinite-
 520 length output string, and the caller simply uses as many bits of the output string as are needed.
 521

522 **7 Implementation Considerations**523 **7.1 Precomputation**

524 cSHAKE is defined to fill one entire call⁵ to the underlying KECCAK- f function [1] with the byte
525 string resulting from encoding and padding the customization string S and the name string N (see
526 Sec. 3.3). However, an implementation can precompute the result of processing this padded
527 block with cSHAKE, and thus, will suffer no performance penalty when reusing the same
528 choices of S and N in multiple cSHAKE executions. Since TupleHash, and ParallelHash are
529 defined in terms of cSHAKE, this same precomputation is available to implementations of those
530 functions, as well.

531 KMAC can precompute the result of hashing S and N , and the result of hashing the key K . Thus,
532 KMAC128 using a fixed, precomputed customization string and key will process an input string
533 as efficiently as SHAKE128.

534 **7.2 Limited Implementations**

535 The cSHAKE, KMAC, TupleHash, and ParallelHash functions are defined to accept a wide
536 range of possible inputs (including unreasonably long inputs, and inputs including fractional
537 bytes), and to produce a wide range of possible output lengths. However, it is acceptable for a
538 specific implementation to limit the possible inputs that it will process, and the allowed output
539 lengths that it will produce.

540 For example, it is acceptable to limit an implementation of any of these functions to producing
541 no more than 65536 bytes of output, or to producing only whole bytes of output, or to accepting
542 only byte strings (never fractional bytes) as inputs. Additionally, implementations intended for
543 only a specific, limited use may further restrict the sets of inputs they will process. For example,
544 an implementation of TupleHash256 used only to process a 6-tuple of strings, and always using a
545 customization string of "address tuple", would be acceptable.

546 If it is possible for an implementation of one of these functions to be given a set of inputs that it
547 cannot process, then the implementation shall signal an error condition and refuse to produce an
548 output.

549 **7.3 Exploiting Parallelism in ParallelHash**

550 Specific implementations of ParallelHash are permitted to restrict their implementation to a small
551 subset of the allowed values. For example, it would be acceptable for a particular implementation
552 to only allow a single value of B if it were only expected to interoperate with another
553 implementation that similarly restricted B to that same value.

⁵ Each call to the underlying KECCAK- f function processes r bits, where r is the *rate* parameter. For cSHAKE128, r = 1344 bits; for cSHAKE256, r = 1088 bits.

554 ParallelHash can be implemented in a straightforward and reasonably efficient way even when
555 only sequential processing is available. However, a much faster implementation is possible when
556 each of the individual blocks of the message can be handled in parallel. The choice of block size
557 B can have a huge impact on the efficiency of ParallelHash in this case. ParallelHash is designed
558 so that any machine that can apply parallel processing can, in principle, benefit from that parallel
559 processing; a machine that can hash four blocks in parallel and a machine that can hash 32
560 blocks in parallel can each benefit from all the parallel processing ability that is available.

561

562 **8 Security Considerations**563 **8.1 Security Properties for Name and Customization String**564 **8.1.1 Equivalent Security to SHAKE for Any Legal S and N**

565 For a given choice of S and N , cSHAKE128(X, L, S, N) has exactly the same security properties
 566 as SHAKE128(X, L); and cSHAKE256(X, L, S, N) has exactly the same security properties as
 567 SHAKE256(X, L). There are no "weak" values for S or N .

568 **8.1.2 Different S and N Give Unrelated Functions**

569 Suppose (s_1, n_1) and (s_2, n_2) are two customization and name strings pairs, and either $s_1 \neq s_2$, or
 570 $n_1 \neq n_2$. Furthermore, suppose x_1 and x_2 are input strings, and q_1 and q_2 are lengths of the
 571 requested output. Then, cSHAKE(x_1, q_1, s_1, n_1) and cSHAKE(x_2, q_2, s_2, n_2) are unrelated
 572 functions. That means:

- 573 • Knowledge of a set of outputs of cSHAKE(X, L, s_1, n_1) gives no information about any
 575 output of cSHAKE(X, L, s_2, n_2).
- 576 • The probability that cSHAKE(x_1, q_1, s_1, n_1) and cSHAKE(x_2, q_2, s_2, n_2) have the same
 577 value is 2^{-q_1} .

578 Because KMAC, TupleHash, and ParallelHash are derived from cSHAKE, they inherit these
 579 properties. Specifically:

- 580 • Each of these functions is unrelated to any of the other functions. There is no relationship
 582 between KMAC (for any set of inputs) and TupleHash (for any set of inputs).
- 583 • For any of these functions, using a different customization string gives an unrelated function.
 584 Thus, if $s_1 \neq s_2$, ParallelHash(X, B, L, s_1) and ParallelHash(X, B, L, s_2) are unrelated
 585 functions: knowing the output of one function gives no information about the output of the
 586 other.

588 **8.2 Claimed Security Level**

589 cSHAKE, KMAC, TupleHash, and ParallelHash are all defined for two claimed security levels:
 590 128 bits and 256 bits.

591

592 cSHAKE128, KMAC128, TupleHash128, and ParallelHash128 each provides a security level of
 593 128 bits. This means that, for a given output length L , there is no *generic attack* on one of these
 594 functions requiring less than 2^{128} work that does not also exist for any hash function with the
 595 same output length. Similarly, cSHAKE256, KMAC256, TupleHash256, and ParallelHash256
 596 each provides a security level of 256 bits.

597

598 Note that a claimed security level of 128 bits is a lower bound on its security—under some
 599 circumstances, an algorithm like KMAC128, claiming 128 bits of security, may provide higher
 600 than 128-bit security in practice.

602 **8.3 Collisions and Preimages**

603 All these functions support variable output lengths. The difficulty of an attacker finding a
 604 collision or preimage for any of these functions depends on both the claimed security level and
 605 the output length.

606 A function like cSHAKE128, with a claimed security level of 128 bits, may be vulnerable to a
 607 collision or preimage attack with 2^{128} work regardless of its output length—a longer output does
 608 not, in general, improve its security against these attacks. However, a shorter output makes the
 609 function more vulnerable to these attacks. With an output of L bits, a collision attack will require
 610 about $2^{L/2}$ work, and a preimage attack will require about 2^L work.

611 **8.4 Guidance for Using KMAC Securely**

612 For maximum flexibility and usefulness, the KMAC functions are defined for arbitrary-sized
 613 output lengths and key lengths. However, not all such output and key lengths are secure.

614 **8.4.1 KMAC Key Length**

615 The input key length is the parameter that is most straightforwardly translated into a security
 616 level. Given a small number of known (MAC, plaintext) pairs, an attacker requires at most $2^{\text{len}(K)}$
 617 operations to find the key K .

618 Applications of this Recommendation **shall not** select an input key, K , whose length is less than
 619 their required security level. Guidance for cryptographic algorithm and key-size selection is
 620 available in [4].

621 **8.4.2 KMAC Output Length**

622 The output length is another important security parameter for KMAC—it determines the
 623 probability that an online guessing attack will succeed in forging a MAC tag. In particular, an
 624 attacker will need to submit, on average, 2^L invalid (message, MAC) pairs for each successful
 625 forgery. Since L only affects online attacks, a system that uses KMAC for message
 626 authentication can mitigate attacks that exploit a short L by limiting the total number of invalid
 627 (message, MAC) pairs that can be submitted for verification under a given key.

628 When used as a MAC, applications of this Recommendation **shall not** select an output length L
 629 that is less than 32 bits, and **shall** only select an output length less than 64 bits after a careful risk
 630 analysis is performed.

631 To illustrate the security properties of KMAC for given parameter settings, Table 1 lists other
 632 approved MAC algorithms, CMAC[5] and HMAC[6], along with equivalent settings for KMAC.
 633 Note that equivalent settings do not result in the same output.

634 **Table 1: Equivalent security settings for KMAC and previously standardized MAC algorithms**

| Existing MAC Algorithm | KMAC Equivalent |
|------------------------------|--|
| CMAC (K , text) | KMAC128 (K , text , 128, S) |

| | |
|---------------------------|-------------------------------|
| HMAC-SHA256 ($K, text$) | KMAC256 ($K, text, 256, S$) |
| HMAC-SHA512 ($K, text$) | KMAC256 ($K, text, 512, S$) |

635

636 **Appendix A—KMAC, TupleHash, and ParallelHash in Terms of KECCAK[c]**

637 FIPS 202 specifies the KECCAK[c] function, on which the SHA-3 and SHAKE functions are
 638 built. KMAC, TupleHash, and ParallelHash are defined in terms of cSHAKE, as specified in
 639 Sec. 3. In this appendix, KMAC, TupleHash, and ParallelHash are defined directly in terms of
 640 KECCAK[c]. These definitions are exactly equivalent to the definitions made in terms of
 641 cSHAKE in Secs. 4, 5, and 6.

642 **KMAC128(K, X, L, S):**

643 *Validity Conditions:* $\text{len}(K) < 2^{2040}$ and $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 644
- 645 1. $\text{new}X = \text{bytepad}(\text{encode_string}(K), 168) \parallel X \parallel \text{right_encode}(L).$
 - 646 2. $T = \text{bytepad}(\text{encode_string}(S) \parallel \text{encode_string}(\text{"KMAC"}), 168).$
 - 647 3. return KECCAK[256]($T \parallel \text{new}X \parallel 00, L$).

648 **KMAC256(K, X, L, S):**

649 *Validity Conditions:* $\text{len}(K) < 2^{2040}$ and $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 650
- 651 1. $\text{new}X = \text{bytepad}(\text{encode_string}(K), 136) \parallel X \parallel \text{right_encode}(L).$
 - 652 2. $T = \text{bytepad}(\text{encode_string}(S) \parallel \text{encode_string}(\text{"KMAC"}), 136).$
 - 653 3. return KECCAK[512]($T \parallel \text{new}X \parallel 00, L$).

654 **TupleHash128(X, L, S):**

655 *Validity Conditions:* $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 656
- 657 1. $z = "".$
 - 658 2. $n =$ the number of input strings in the tuple X .
 - 659 3. for $i = 1$ to n :
 $z = z \parallel \text{encode_string}(X[i]).$
 - 660 4. $\text{new}X = z \parallel \text{right_encode}(L).$
 - 661 5. $T = \text{bytepad}(\text{encode_string}(S) \parallel \text{encode_string}(\text{"TupleHash"}), 168).$
 - 662 6. return KECCAK[256]($T \parallel \text{new}X \parallel 00, L$).

664 **TupleHash256(X, L, S):**

665 *Validity Conditions:* $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

- 666
- 667 1. $z = "".$
 - 668 2. $n =$ the number of input strings in the tuple X .
 - 669 3. for $i = 1$ to n :
 $z = z \parallel \text{encode_string}(X[i]).$
 - 670 4. $\text{new}X = z \parallel \text{right_encode}(L).$
 - 671 5. $T = \text{bytepad}(\text{encode_string}(S) \parallel \text{encode_string}(\text{"TupleHash"}), 136).$
 - 672 6. return KECCAK[512]($T \parallel \text{new}X \parallel 00, L$).

674 **ParallelHash128(X, B, L, S):**

675 *Validity Conditions:* $0 < B < 2^{2040}$ and $\lceil \text{len}(X)/B \rceil < 2^{2040}$ and
 676 $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

677
 678 1. $n = \lceil (\text{len}(X)/8) / B \rceil$.
 679 2. $z = \text{left_encode}(B)$.
 680 3. for $i = 0$ to $n-1$:
 $z = z \parallel \text{KECCAK}[256](\text{substring}(X, i*B*8, (i+1)*B*8) \parallel 1111, 256)$.
 682 4. $z = z \parallel \text{right_encode}(n) \parallel \text{right_encode}(L)$.
 683 5. $\text{new}X = z$.
 684 6. $T = \text{bytepad}(\text{encode_string}(S) \parallel \text{encode_string}(\text{"ParallelHash"}), 168)$.
 685 7. return $\text{KECCAK}[256](T \parallel \text{new}X \parallel 0\ 0, L)$.

686 **ParallelHash256(X, B, L, S):**

687 *Validity Conditions:* $0 < B < 2^{2040}$ and $\lceil \text{len}(X)/B \rceil < 2^{2040}$ and
 688 $0 \leq L < 2^{2040}$ and $\text{len}(S) < 2^{2040}$

689
 690 1. $n = \lceil (\text{len}(X)/8) / B \rceil$.
 691 2. $z = \text{left_encode}(B)$.
 692 3. for $i = 0$ to $n-1$:
 $z = z \parallel \text{KECCAK}[512](\text{substring}(X, i*B*8, (i+1)*B*8) \parallel 1111, 512)$.
 694 4. $z = z \parallel \text{right_encode}(n) \parallel \text{right_encode}(L)$.
 695 5. $\text{new}X = z$.
 696 6. $T = \text{bytepad}(\text{encode_string}(S) \parallel \text{encode_string}(\text{"ParallelHash"}), 136)$.
 697 7. return $\text{KECCAK}[512](T \parallel \text{new}X \parallel 0\ 0, L)$.

698

699 **Appendix B—Hashing into a Range (Informative)**

700 Hash functions with variable-length output like cSHAKE, KMAC, TupleHash, and ParallelHash
 701 can easily be used to generate an integer X within the range $0 \leq X < R$, denoted as $0..R-1$ in this
 702 document, for any R . The following method will produce outputs that are extremely close to a
 703 uniformly distribution over that range.

704 In order to hash into an integer in the range $0..R-1$, do the following:

- 705
- 706 1. Let $k = \lceil \lg(R) \rceil + 128$.
 - 707 2. Call the hash function with a requested length of at least k bits. Let the resulting bit string be
 708 Z .
 - 709 3. Let $N = \text{bits_to_integer}(Z) \bmod R$.

710

711 N now contains an integer that is extremely close to being uniformly distributed in the range
 712 $0..R-1$. For any t such that $0 \leq t < R$, the following statement is true.

713

714 $\text{Prob}(t) - 1/R \leq 2^{-128}$.

715

716 This technique can be applied to SHAKE, cSHAKE, KMAC, TupleHash, or ParallelHash
 717 whenever an integer within a specific range is needed, so long as it is acceptable for the resulting
 718 integer to have this very small deviation from the uniform distribution on the integers $\{0, 1, \dots,$
 $R-1\}$.

719

720

721 This technique depends on a method to convert a bit string to an integer, called `bits_to_integer()`
 722 above.

723

724 **bits_to_integer** (b_1, b_2, \dots, b_n):

725 1. Let (b_1, b_2, \dots, b_n) be the bits of a bit string from the most significant to the least significant
 726 bits.

727 2. $x = \sum_{i=1}^n 2^{(n-i)} b_i$

728 3. Return (x) .

729

Appendix C—References

- [1] National Institute of Standards and Technology, *SHA-3 Standard: Permutation-Based Hash and Extendable-Output Functions*, Federal Information Processing Standards (FIPS) Publication 202, August 2015, 37 pp. <http://dx.doi.org/10.6028/NIST.FIPS.202>.
- [2] G. Bertoni, J. Daemen, M. Peeters, and G. Van Assche, *The KECCAK reference, version 3.0*, January 14, 2011, 69 pp. <http://keccak.noekeon.org/Keccak-reference-3.0.pdf> [accessed 6/14/2016].
- [3] G. Bertoni, J. Daemen, M. Peeters, and G. Van Assche, *Cryptographic sponge functions, version 0.1*, January 14, 2011, 93 pp. <http://sponge.noekeon.org/CSF-0.1.pdf> [accessed 6/14/2016].
- [4] E. Barker, *Recommendation for Key Management, Part 1: General*, NIST Special Publication (SP) 800-57 Part 1 Revision 4, National Institute of Standards and Technology, January 2016, 160 pp. <http://dx.doi.org/10.6028/NIST.SP.800-57pt1r4>.
- [5] M. Dworkin, *Recommendation for Block Cipher Modes of Operation: the CMAC Mode for Authentication*, NIST Special Publication (SP) 800-38B, National Institute of Standards and Technology, May 2005, 29 pp. <http://dx.doi.org/10.6028/NIST.SP.800-38B>.
- [6] National Institute of Standards and Technology, *The Keyed-Hash Message Authentication Code (HMAC)*, Federal Information Processing Standards (FIPS) Publication 198-1, July 2008, 13 pp. http://csrc.nist.gov/publications/fips/fips198-1/FIPS-198-1_final.pdf [accessed 6/14/2016].